

Then the cartesian coordinates  $(x,y,z)$ , the cylindrical coordinates  $(r,\theta,z)$ , and the spherical coordinates  $(\rho,\varphi,\theta)$  of a point are related as follows:

$$\text{cart} \leftrightarrow \text{cyl} \quad \begin{cases} x = r \cos \theta, \\ y = r \sin \theta, \end{cases} \quad \begin{cases} r = \sqrt{x^2 + y^2}, \\ \theta = \arctan \frac{y}{x}, \end{cases} \quad \begin{cases} \sin \theta = \frac{y}{\sqrt{x^2 + y^2}}, \\ \cos \theta = \frac{x}{\sqrt{x^2 + y^2}}. \end{cases}$$

$$\text{cyl} \leftrightarrow \text{sph} \quad \begin{cases} r = \rho \sin \phi, \\ z = \rho \cos \phi, \end{cases} \quad \begin{cases} \rho = \sqrt{r^2 + z^2}, \\ \phi = \arctan \frac{r}{z}, \end{cases} \quad \begin{cases} \sin \phi = \frac{r}{\sqrt{r^2 + z^2}}, \\ \cos \phi = \frac{z}{\sqrt{r^2 + z^2}}. \end{cases}$$

$$\text{cart} \leftrightarrow \text{sph} \quad \begin{cases} x = \rho \cos \theta \sin \phi, \\ y = \rho \sin \theta \sin \phi, \\ z = \rho \cos \phi, \end{cases} \quad \begin{cases} \rho = \sqrt{x^2 + y^2 + z^2}, \\ \theta = \arctan \frac{y}{x}, \\ \phi = \arctan \frac{\sqrt{x^2 + y^2}}{z} \\ = \arccos \frac{z}{\sqrt{x^2 + y^2 + z^2}}. \end{cases}$$